

Loading Surface in the Course of Mechanical-Thermal Treatment and Steady-State Creep of Metals

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Abstract: Kinetics of the loading surface of a material gives precious information on the level of the hardening of the material. This paper is concerned with the evolution of the loading surface during successive actions, such as: (i) plastic deformation, (ii) annealing of the pre-strained specimen, and (iii) secondary creep of the treated material. The analysis of the loading surface is carried out in terms of the synthetic theory of irrecoverable deformation.

Keywords: loading surface; mechanical-thermal treatment; creep and plastic strain; synthetic theory of irrecoverable deformation

1 Introduction

Numerous experiments testify that mechanical-thermal treatment (MTT) is an effective tool to improve the strength of metals [2, 4, 9, 10]. MTT involves (i) plastic deformation of a specimen at room temperature (T_0), e.g. in uniaxial tension (we give the acting stress symbol σ_{x_0} and we will mark as ε_{x_0} the plastic strain induced by σ_{x_0}), and (ii) annealing of the cold-worked specimen in unloaded state (let us denote the annealing temperature and duration as T_1 and t_1 , respectively). As seen in Figures 1 and 2, if we subject the treated specimens to creep with stress σ_x and temperature T_2 , the creep rate ($\dot{\varepsilon}_x$) is not a monotonous function of the plastic pre-strain ε_{x_0} (with the proviso that the values of σ_x , T_2 , T_1 , and t_1 are unchangeable). Figure 1 demonstrates the steady-state creep rate $\dot{\varepsilon}_x$ ($\sigma_x = 25$ MPa, $T_2 = 700^\circ\text{C}$) of Ni+1.18% alloy against plastic pre-strain at room temperature $\dot{\varepsilon}_{x_0}$ developed in the course of preliminary MTT (the annealing temperature and duration $T_1 = T_2 = 700^\circ\text{C}$ and $t_1 = 1$ hour,

respectively). Figure 2 shows the steady-state creep rate ($\sigma_x = 15 \text{ MPa}$, $T_2 = 500^\circ\text{C}$) of copper as a function of plastic pre-strain at room temperature developed in MTT ($T_1 = T_2 = 500^\circ\text{C}$, $t_1 = 1 \text{ hour}$). In these figures, the points are the experiment [2,4], and the solid line is the analytical curve.

According to Figures 1 and 2, there exists an optimal level of plastic pre-straining after which (with intermediate annealing) the rate of stationary creep is minimal. The existence of different types of behavior of the tested specimens subjected to creep is connected with distinctions in the initial structure of the material formed as a result of plastic pre-straining and annealing. Indeed, the structure affects the intensity of the processes of polygonization and recrystallization, which control the rate of stationary creep.

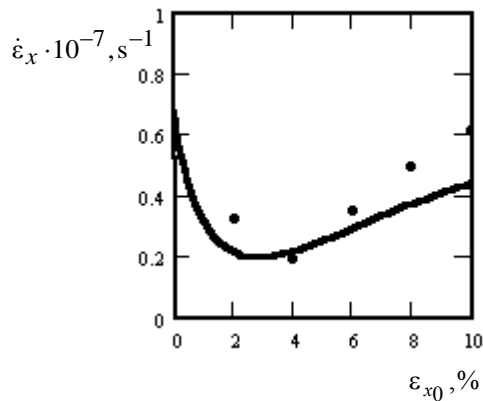


Figure 1

Steady-state creep rate of Ni+1.18% alloy against plastic pre-strain

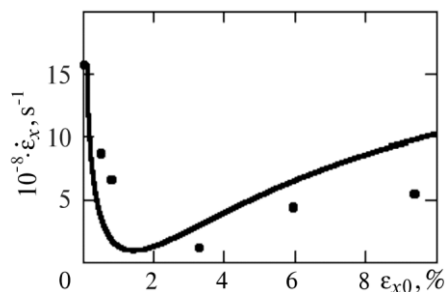


Figure 2

Dependence of the steady-state creep rate of copper on the level of preliminarily induced plastic strains

Another positive effect of MTT is an increase in the duration of the secondary creep [2,4], which can be concluded from cavities nucleation and development [3].

Due to a plastic strain, the initial (relatively perfect) crystals suffer fragmentation and the sizes and orientation of fragments depend on the level of strains. The boundaries between the fragments form a three-dimensional grid of dislocations which can be regarded as a pileup of dislocations. Subsequent annealing ambiguously affects the preliminarily formed dislocation structure promoting the initiation of the thermally controlled processes of polygonization and recrystallization. The course of one of these processes depends on the level of pre-straining and the temperature of annealing [5-7, 12].

In the case of annealing of an insignificantly cold-hardened material, we observe the redistribution of dislocations of the same sign in the form of rearrangement into vertical walls. As a result, poorly formed cells appearing as a result of plastic deformation become completely surrounded with low-angle boundaries and gradually turn into well-formed subgrains in the body of which the density of dislocations is lower than in the deformed matrix. The higher (to a certain degree) the value of plastic pre-straining, the greater the number of appearing subgrains, i.e., the higher the intensity of polygonization. The polygonized structure formed in the process of preliminary TMT decreases the level of sliding (both coarse and fine) in testing for creep. This fact can be explained by the restriction of the free path of dislocations imposed by the preliminarily formed grid of subgrain boundaries.

In the case of annealing of a material with relatively high plastic strains, the density of dislocations built in the subgrain boundaries increases and, hence, the angle of their mutual orientation also increases. It is known that subgrains with large-angle boundaries play the role of centers of recrystallization, i.e., of the formation and growth of grains with more perfect structure. In the course of recrystallization, the resistance of the metal to plastic deformation significantly decreases since the rapid migration of the boundaries intensely "cleans" the deformed matrix, which facilitates the motion of dislocations under conditions of creep and increases the rate of stationary creep as compared with its optimal value. Thus, the optimal degree of plastic pre-straining should be chosen to avoid the possibility of intense recrystallization.

Classic theories such as ageing (time-hardening) theory, flow theory, and strain-hardening theory [1] are incapable of the modeling of the dependence $\dot{\epsilon}_x = f(\epsilon_{x0})$ due to the fact that, in terms of these theories, the creep rate is related to the acting stresses and the loading-prehistory is ignored. This fact motivates the author to model the effect of MTT utilizing a more efficient model able to embrace a wider circle of processes and their interplay: the synthetic theory of irrecoverable deformation (ST).

2 Mathematical Apparatus: Synthetic Theory

The analytical description of the dependence of steady-state creep rate $\dot{\varepsilon}_x$ on the plastic pre-strain ε_{x_0} in the course of MTT is carried out in terms of the synthetic theory of irrecoverable deformation [8-11]. The yield limit of a material in the three-dimensional subspace (\mathbf{R}^3) of five-dimensional stress deviator space has the shape of a sphere, which correspond to the von-Mises yield criterion:

$$S_1^2 + S_2^2 + S_3^2 = 2/3 \sigma_T^2 \quad (1)$$

where σ_T , depending on the problem considered, is the yield limit (σ_S) or the creep limit (σ_S) of the material; S_i ($i = 1, 2, 3$) are coordinate axes in \mathbf{R}^3 .

In terms of ST, the yield/loading surface is constructed as the inner envelope of tangent planes. In the virgin state, sphere (1) is the inner envelope of tangent planes, which are equidistant to the origin of coordinate in all directions. A loading is presented by a stress-vector, \vec{S} , whose components are defined in [8, 11]. As the stress-vector grows, it translates on its endpoint tangent planes (the orientation of tangent plane does not vary during the motion). The planes which are not reached by \vec{S} remain stationary. The displacement of a plane symbolizes the increment in plastic deformation (plastic slip) within an appropriate slip system at a point of a body. The plastic strain developed within one slip system defines a microlevel of deformation. The total strain (macrostrain) is calculated by the summation (threefold integrals) of the microstrains occurring in activated slip systems.

Consider the case of uniaxial tension when the components of \vec{S} are $S_1 = \sqrt{2/3} \sigma_x$, $S_2 = 0$, $S_3 = 0$ [8]. As $|\vec{S}| = \sqrt{2/3} \sigma_S$, there is only one plane tangential to the sphere (1) reached by the vector \vec{S} , and it is perpendicular to the \vec{S} . During further elongation of the \vec{S} , new planes become located on the endpoint of the stress-vector and – following the rule that a loading surface is the inner envelope of planes – the loading surface take the shape of a cone symmetric relative to the S_1 -axis, and its generator is constituted of the boundary tangent planes reached by the stress-vector. This cone goes over to the initial sphere in the directions where tangent planes remain immovable.

The plastic strain component in uniaxial tension, e_1 , is calculated as [8-11]

$$e_1 = \frac{1}{r} \int_{\alpha} \int_{\beta} \int_{\lambda} \varphi_N \sin \beta \cos \beta \cos \lambda d\beta d\lambda, \quad e_2 = 0, \quad e_3 = 0, \quad (2)$$

where φ_N is referred to as irrecoverable strain intensity (index N stands for the vector normal to the tangent plane, which gives the orientation of the plane), which is defined by the following differential equation

$$d\psi_N = r d\varphi_N - K\psi_N dt, \quad (3)$$

where φ_N is called defects intensity; dt is the time differential, r is the constant of material, and K is a function of the homological temperature and current stresses:

$$K = K_1 \exp(K_2 \Theta) (\sqrt{2/3} \sigma_x)^{K_3}, \quad (4)$$

where K_i ($i=1,2,3$) are the material constants.

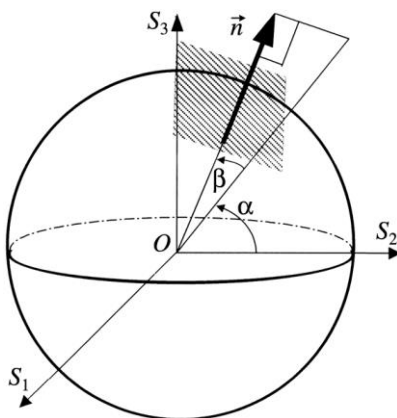


Figure 3
Orientation of the normal \vec{n} in the subspace \mathbf{R}^3

The defects intensity, according to [8, 9], is

$$\psi_N = H_N^2 - 2/3 \sigma_T^2, \quad H_N = \vec{S} \cdot \vec{N} = \vec{S} \cdot \vec{n} \cos \lambda = 2/3 \sigma_x \sin \beta \cos \lambda, \quad (5)$$

where H_N ($i=1,2,3$) is a distance to the plane reached by stress-vector; angle β gives the orientation of a plane in \mathbf{R}^3 (the role of angle λ , which is immaterial within this article, can be found in [8]). In general, the orientation of the normal in \mathbf{R}^3 , $\vec{n}(\sin \beta, \cos \alpha \cos \beta, \sin \alpha \cos \beta)$, is shown in Figure 3. The magnitude of H_N shows the degree of the hardening of material. Actually, the greater the H_N , the greater the stress-vector needed to reach the plane.

When calculating “immediate” plastic deformation ($dt = 0$), the formula takes the form

$$\psi_N = r\varphi_N. \quad (6)$$

For the case of secondary creep ($\dot{\psi}_N = 0$), from (3) we have

$$\dot{\phi}_N = K\psi_N / r. \quad (7)$$

The steady-state creep rate strain component is expressed by the relationship where the integrand is $\dot{\phi}_N$.

If annealing a work-hardened specimen in an unloaded state ($d\phi = 0$), the formula yields

$$d\psi_N = -K\psi_N dt. \quad (8)$$

The solution of differential equation (8) is

$$\psi_N = \psi_{N_0} \exp(-Kt),$$

where ψ_{N_0} is the defects intensity in the work-hardened material. Therefore, on account of formula (5), the distance to the planes after the plastic deformation and annealing is

$$H_N^2 = \psi_{N_0} \exp(-Kt) + 2/3 \sigma_T^2. \quad (9)$$

Formula (9) expresses the motion of the planes toward the origin of coordinates. This motion for each plane will terminate as it touches the sphere (1).

3 The Generalization of the Synthetic Theory to the Case of MTT

To evaluate the steady-state creep rate of a metal after MTT, we replace formulae (5) and (4) by

$$\psi_{MN} = H_N^2 - H_{TN}^2, \quad (10)$$

$$K_M = f(\Theta, H_{\max}) = K_1 \exp(K_2 \Theta) H_{\max}^{K_3}, \quad (11)$$

where H_{TN} is the distance to a plane after MTT, which characterizes the thermal stability of the polygonization structure against the recrystallization during creep. In the absence of MTT, $H_{TN} = \sqrt{2/3} \sigma_P$ and the relation for ψ_{MN} from (10) degenerates to (5). In formula (10), H_{\max} is the maximal distance to planes for the whole loading history at a given temperature.

3.1 Tension of Specimen at Room Temperature

The plastic strain component, e_{10} , is calculated as [8]

$$e_{10} = a_0 \Phi(\sin \beta_{10}), \quad a_0 = \pi \sigma_S^2 / (9r), \quad \sin \beta_{10} = \sigma_S / \sigma_{x_0}, \quad (12)$$

$$\Phi(\xi) = \left(2\sqrt{1-\xi^2} - 5\xi^2\sqrt{1-\xi^2} + 3\xi^4 \ln \frac{1+\sqrt{1-\xi^2}}{\xi} \right) \frac{1}{\xi^2}. \quad (13)$$

The loading surface is shown in Figure 4a. The value of H_{\max} in the plastic loading can be obtained from (5) at $\beta = \pi/2$, $\lambda = 0$.

3.2 Annealing of Deformed Specimen

Consider the case when the annealing temperature coincides with the temperature of the following creep: $T_1 = T_2$.

As seen from (5), the heating of the specimen to the temperature T_1 results in a decrease of H_N due to a drop in the value of σ_T caused by the temperature gradient. Since the temperatures of annealing and creep are assumed to be equal, the effect of MTT on the steady-state creep rate can be revealed by studying the positions of tangent planes relative to the value of σ_P at $T = T_1$. If we ignore an immaterial duration of the heating from T_0 to T_1 , the decrease in H_N can be assumed to be of a step-wise nature, which symbolizes the step-wise motions of planes toward the origin of coordinates. This fact means that the values of angles λ_{10} and β_{10} remain unchangeable during annealing. Therefore, formula (9) at $t = 0$ takes the form

$$H_N^2 = \frac{2}{3} \begin{cases} \left[(\sigma_{x_0} \sin \beta \cos \lambda)^2 - \sigma_S^2 \right] + \sigma_P^2, & \beta_{10} \leq \beta \leq \pi/2, & 0 < \lambda < \lambda_{10} \\ \sigma_P^2, & -\pi/2 < \beta < \beta_{10}, & \lambda_{10} < \lambda \end{cases}. \quad (14)$$

Consider the distance from the origin of coordinates to the point of intersection of tangent plane with S_1 -axis, $L(\beta, \lambda, t)$. For simplicity, while not distorting the result, we study the value of L at $\lambda = 0$. From Figure 4a it follows that

$$L(\beta, t) = H_N / \sin \beta. \quad (15)$$

In active loading, $L(\beta) = \text{const} = \sqrt{2/3} \sigma_{x_0}$ for $\beta_{10} \leq \beta \leq \pi/2$. The value of L due to the temperature decrease, $\Delta T = T_1 - T_0$, according to (14) and (15), is

$$[L(\beta, t=0)]^2 = \frac{2}{3} \left[\sigma_{x_0}^2 - \left(\sigma_S^2 - \sigma_P^2 \right) / \sin^2 \beta \right], \quad \beta_{1_0} \leq \beta \leq \pi/2. \quad (16)$$

As seen from formula (16), the loading surface maintains its shape but the tangent planes from the range $\beta_{1_0} < \beta \leq \pi/2$ are not on the cone tip (Figure 4b).

During annealing, according to (9), (11), and (15), we have

$$H_N^2 = \frac{2}{3} \left[\left(\sigma_{x_0}^2 \sin^2 \beta - \sigma_S^2 \right) \exp(-K_M t) + \sigma_P^2 \right]. \quad (17)$$

$$[L(\beta, t)]^2 = \frac{2}{3} \left[\sigma_{x_0}^2 \exp(-K_M t) - \left(\sigma_S^2 \exp(-K_M t) - \sigma_P^2 \right) / \sin^2 \beta \right], \quad \beta_{1_0} \leq \beta \leq \pi/2. \quad (18)$$

Distance H_{T_N} is determined by Eq. (17) at $t = t_1$.

The presence of K_M in (17) makes it possible to describe the displacement of planes even in a load-free state. Indeed, since the distance H_{\max} appearing in the definition of K_M (14) is non-zero ($H_{\max} = \sigma_{x_0} \neq 0$), formula (17) governs the displacement of planes during the annealing as $\sigma_x = 0$. Another important feature of K_M is that the intensity of the displacements depends, via σ_{x_0} , on the level of plastic pre-strain.

The behavior of function $L(\beta)$ at $t = t_1$ depends on the relationships between the values of $\sigma_S^2 \exp(-K_M t_1)$ and σ_P^2 . If $\sigma_S^2 \exp(-K_M t_1) > \sigma_P^2$, $L(\beta)$ grows with increasing β , $L'(\beta) > 0$. Otherwise, $L(\beta)$ is a decreasing function of β .

The fact that $L'(\beta) > 0$ means that, during the annealing, the planes from the directions $\beta_{1_0} < \beta \leq \pi/2$ travel such distances toward the origin of coordinates that their points of intersection with S_1 -axis lie to the right to the cone tip.

Therefore, it can be concluded that the loading surface at the end of annealing ($t = t_1$) retains the shape formed at $t = 0$.

If $\sigma_S^2 \exp(-K_M t_1) = \sigma_P^2$, $L(\beta) = \text{const}$, i.e. the loading surface has a form of cone on whose tip there are all the planes that were reached by stress vector at plastic loading. The decreasing dependence of $L(\beta)$ on β means that the loading surface, being the inner envelope of tangent planes, loses the angular point (Figure 4c).

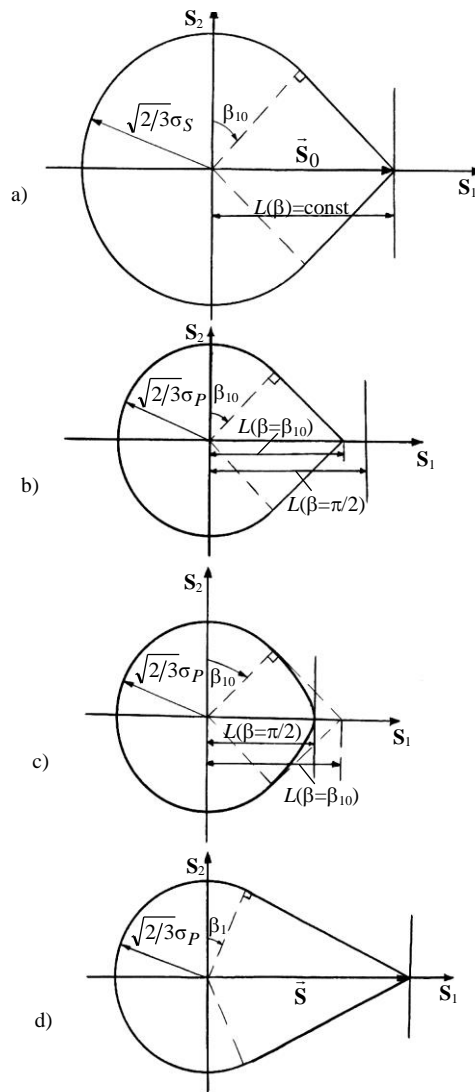


Figure 4

Evolution of loading surface in the course of preliminary MTT and subsequent creep (boundary planes are shown only)

3.3 Steady-State Creep of Metal Treated by MTT

The loading surface in creep ($\sigma_x(t) = const$), similarly to a plastic deformation, has a shape of a cone (Figure 4d) which does not vary in time. Insert H_{T_N} into (6):

$$\Psi_{MN} = \frac{2}{3} \left\{ \begin{array}{l} (\sigma_x \sin \beta \cos \lambda)^2 - [(\sigma_{x_0} \sin \beta \cos \lambda)^2 - \sigma_S^2] \exp(-K_M t_1) - \sigma_P^2, \quad \Omega_{1_0}(\beta, \lambda), \\ (\sigma_x \sin \beta \cos \lambda)^2 - \sigma_P^2 \quad \Omega_1(\beta, \lambda) \end{array} \right\}, \quad (19)$$

where $\Omega_{1_0}(\beta, \lambda)$ is the range of angles β and λ : $\beta_{1_0} < \beta \leq \pi/2$, $0 < \lambda < \lambda_{1_0}$; $\Omega_1(\beta, \lambda)$ stands for $\beta_1 \leq \beta \leq \beta_{1_0}$, $\lambda_{1_0} \leq \lambda \leq \lambda_1$. Here we restrict ourselves to the case when the creep stress vector \vec{S} is such that the range $\Omega_1(\beta, \lambda)$ is greater than $\Omega_{1_0}(\beta, \lambda)$. As such, the values of λ_1 and β_1 are calculated by equating the Ψ_{MN} and λ_1 from $\Omega_1(\beta, \lambda)$ to zero [8, 11]:

$$\cos \lambda_1(\beta) = \sigma_P / [\sigma_x \sin \beta], \quad \sin \beta_1 = \sigma_P / \sigma_x. \quad (20)$$

It must be noted that the loading surface in creep without preliminary MTT is formed by the same set of tangent planes, $\Omega_1(\beta, \lambda)$. However, the planes from the diapason $\Omega_{1_0}(\beta, \lambda)$ travel greater distances on the endpoint of the \vec{S} than those for the treated material.

The creep strain rate after MMT, \dot{e}_{1M} , is determined by formulae (20), (19), (7), and (2):

$$\dot{e}_{1M} = \frac{4\pi\tilde{K}}{3r} \left\{ \int_0^{\lambda_1} \int_{\beta_1}^{\pi/2} \left\{ (\sigma_x \sin \beta \cos \lambda)^2 - \sigma_P^2 \right\} \sin \beta \cos \beta \cos \lambda d\lambda d\beta - \right. \\ \left. - \exp(-K_M t_1) \int_0^{\lambda_{1_0}} \int_{\beta_{1_0}}^{\pi/2} \left\{ (\sigma_{x_0} \sin \beta \cos \lambda)^2 - \sigma_S^2 \right\} \sin \beta \cos \beta \cos \lambda d\lambda d\beta \right\}. \quad (21)$$

According to (5) and (2), the first integral in (21) gives the creep rate without MTT, $\dot{e}_1 = a\Phi(\sin(\beta_1))$, $a = \pi\sigma_P^2/(9r)$, and the second one does the preliminary plastic strain e_{1_0} (formulae (12) and (13)). Therefore,

$$\dot{e}_{1M} = \dot{e}_1 - \tilde{K} \exp[-K_M (e_{1_0} t_1)] \cdot e_{1_0}, \quad (22)$$

where the $\tilde{K} = const$ is obtained from Eq. (11) at $H_{\max} = \sqrt{2/3}\sigma_x = const$.

For the case when MTT is not carried out, we have $e_{10} = 0$ and $\dot{e}_{1M} = \dot{e}_1$. With an increase of pre-strain, the term $\tilde{K} \exp[-K_M(e_{10})t_1] \cdot e_{10}$ first increases and then tends to zero.

On the basis of formula (22), in Figure 1 and 2, the analytical and experimental [2, 4] curves $\dot{e}_{1M} = f(e_{10})$ are plotted. Good agreement between the analytical and experimental data enables us to use formula (22) to predict the steady-state creep of metals as a function of preliminary plastic deformation in the course of MTT.

Conclusions

The analysis of the evolution of loading surface in the course of mechanical-thermal treatment and subsequent steady-state creep has been studied. Depending on the value of plastic pre-strain, in the course of MTT, the loading surface can assume a conic or rounded shape. The analytical results give good agreements with experimental data.

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